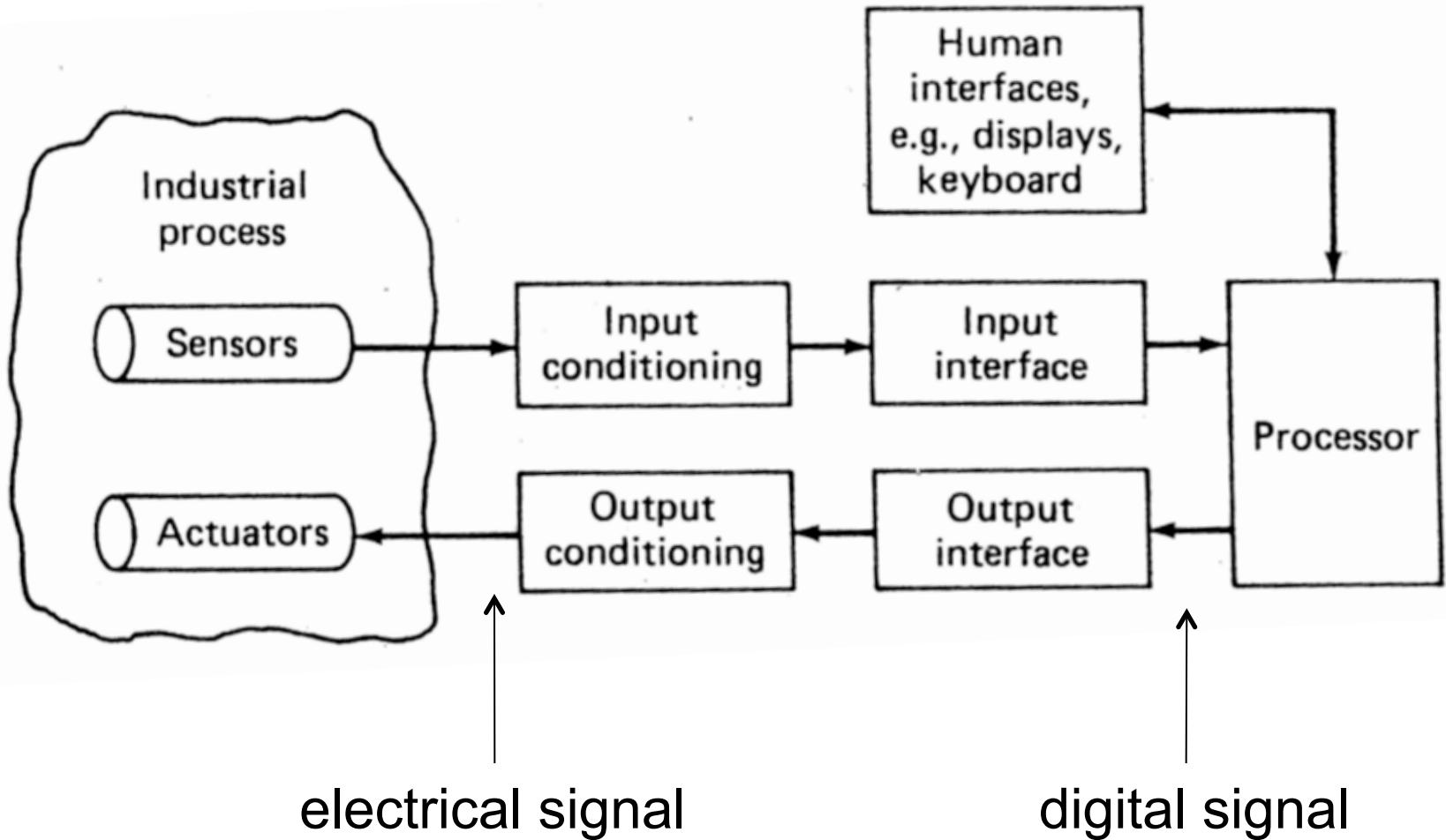


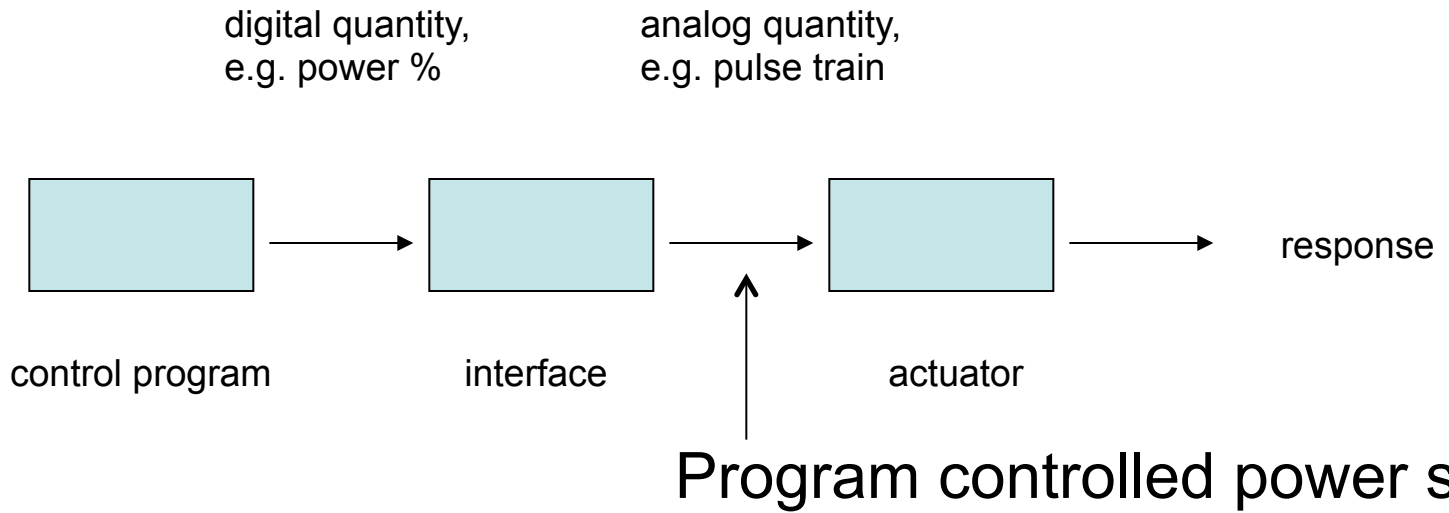
Actuators and acting





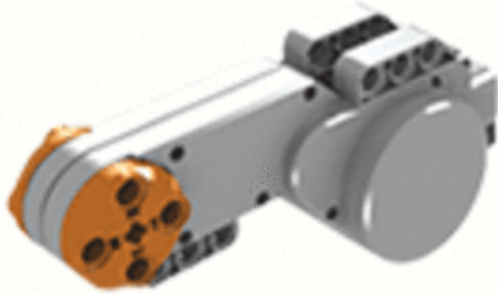
goForward(50)

car drives forward



Open loop control

NXT Actuator

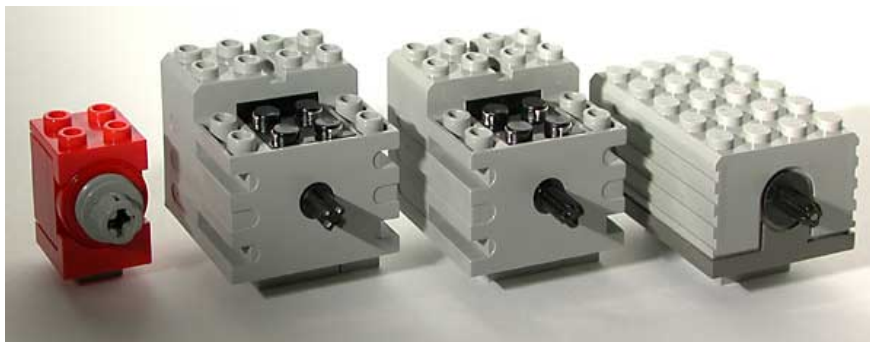
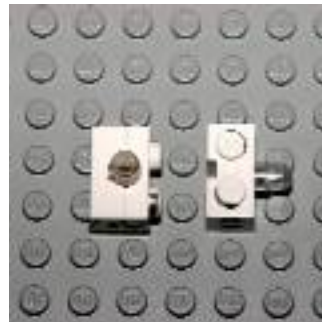


RJ12 connector



6 wire cable

RCX Actuators

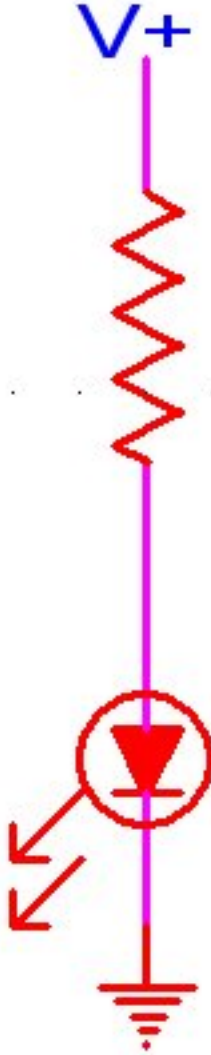


2x2 plate connector



2 wire cable

LED For Dummies



$R1$

$D1$

LED on all the time



R1

D1

S1

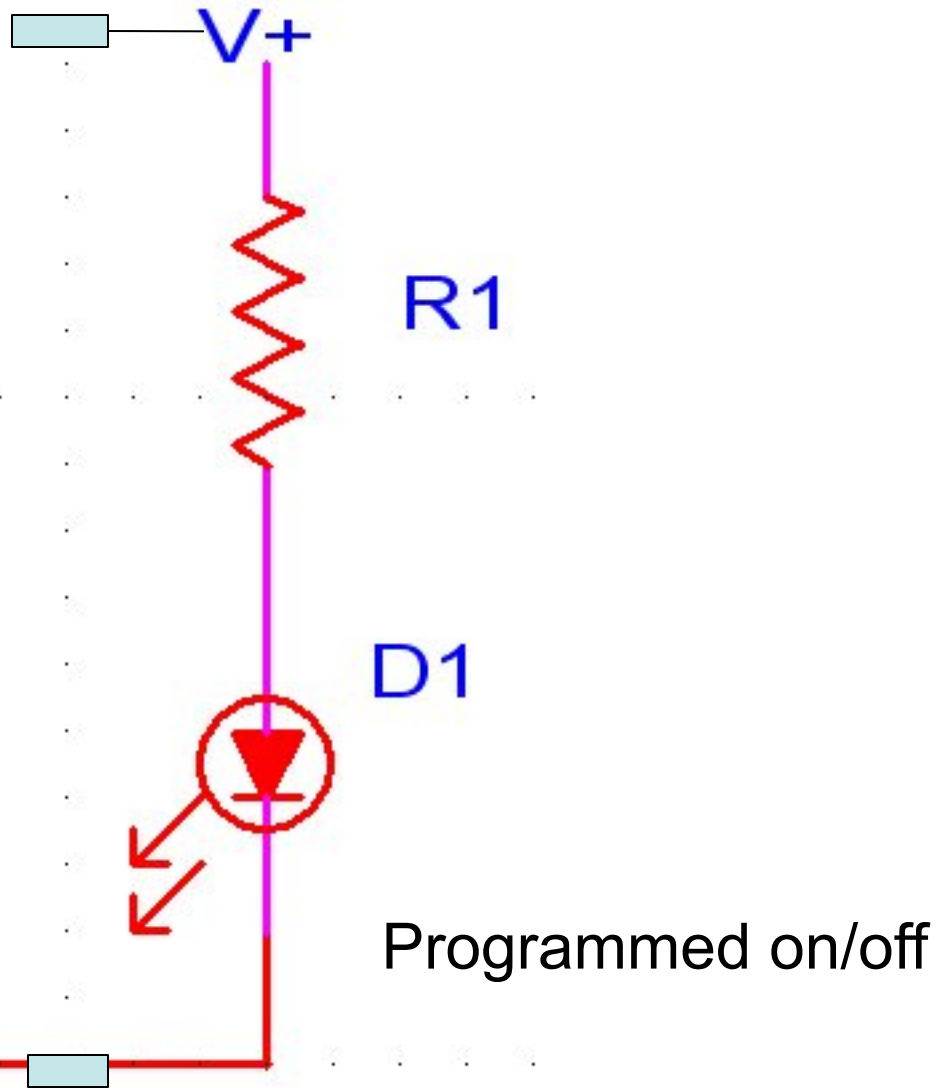
Manually operated switch

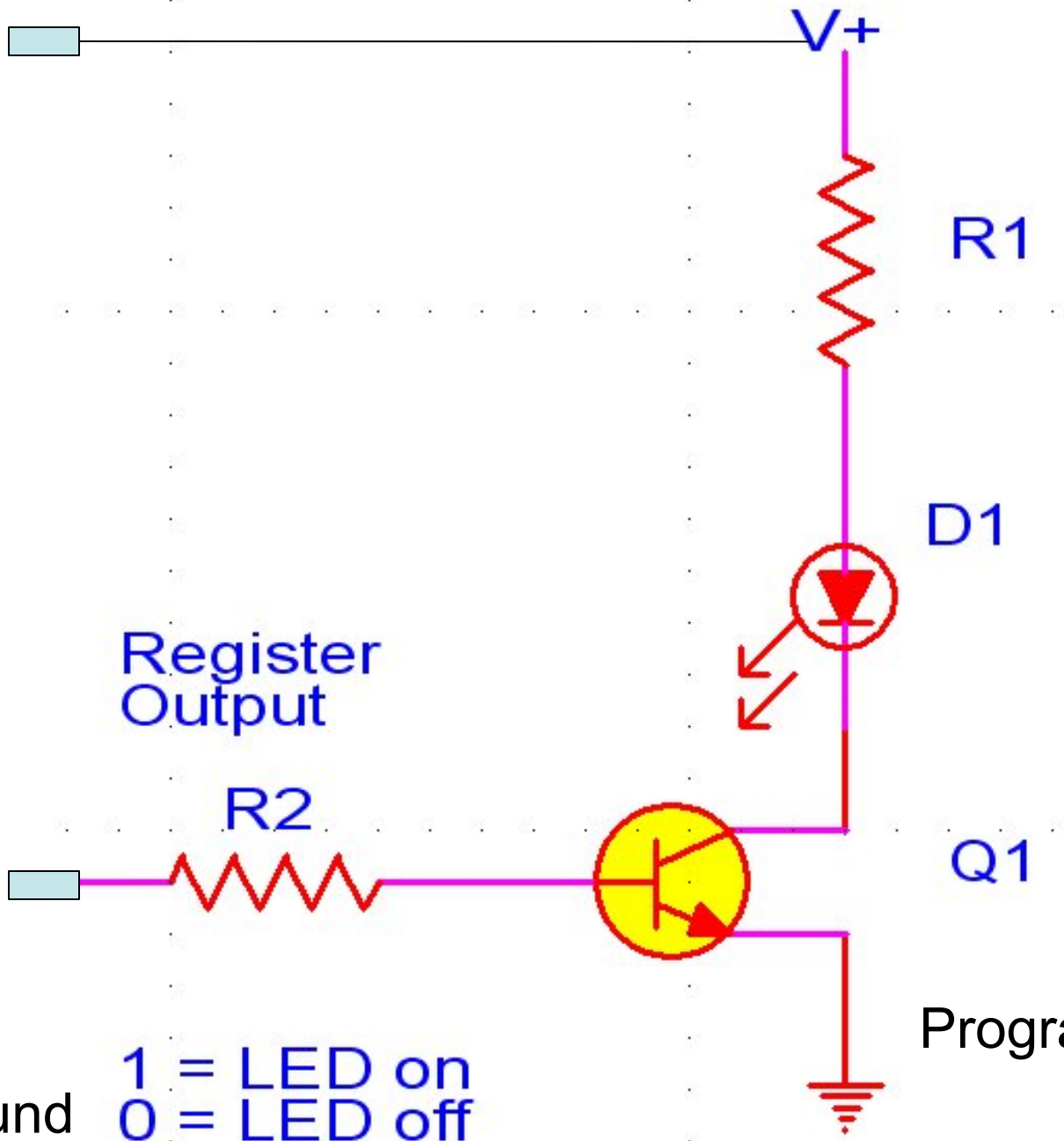
GIO general input/output

Register Output

ground
V+

0 = LED on
1 = LED off



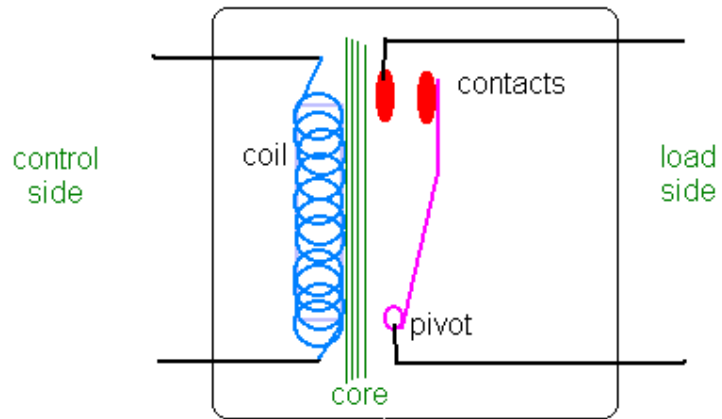


$V+$
ground

1 = LED on
0 = LED off

Programmed on/off

A relay is an electrical switch that opens and closes under the control of another electrical circuit

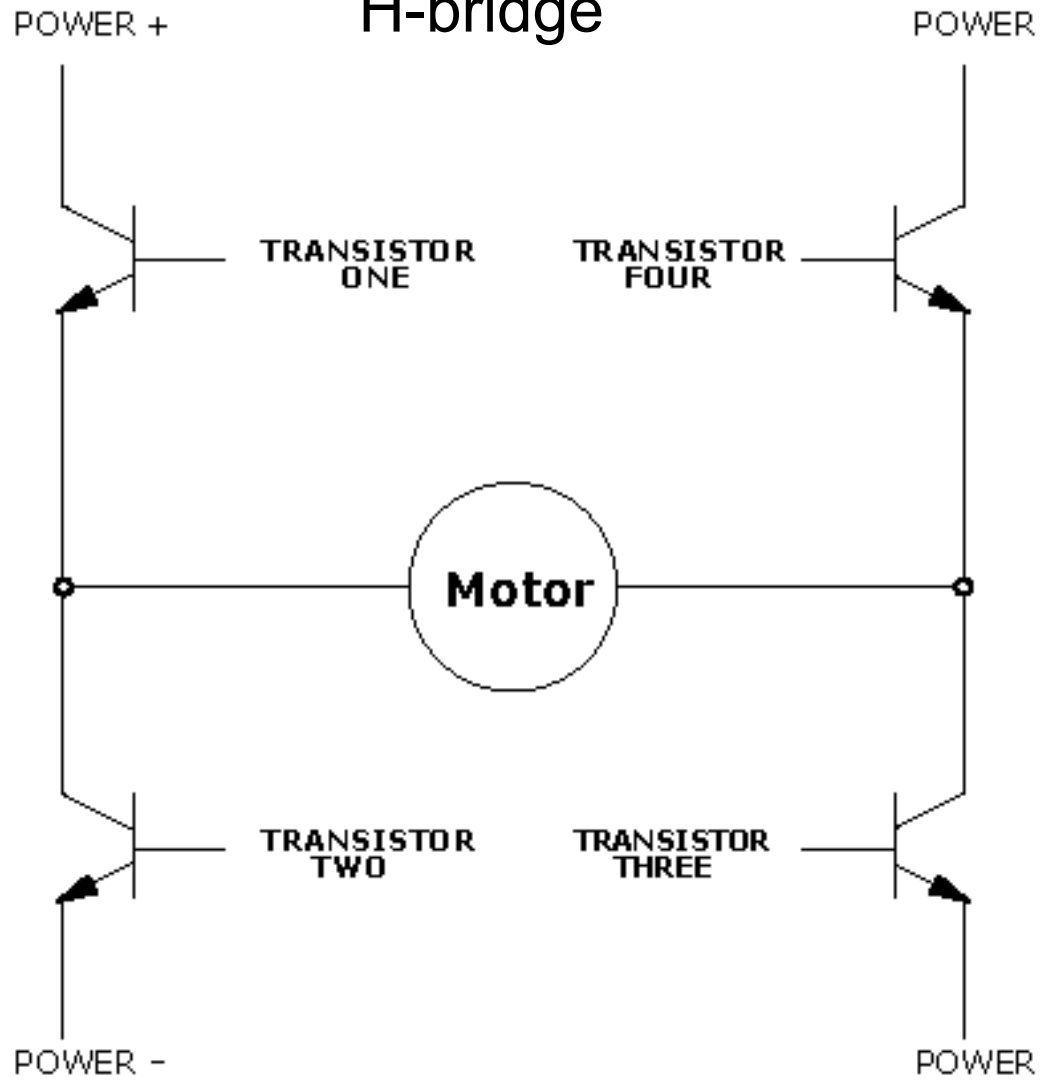


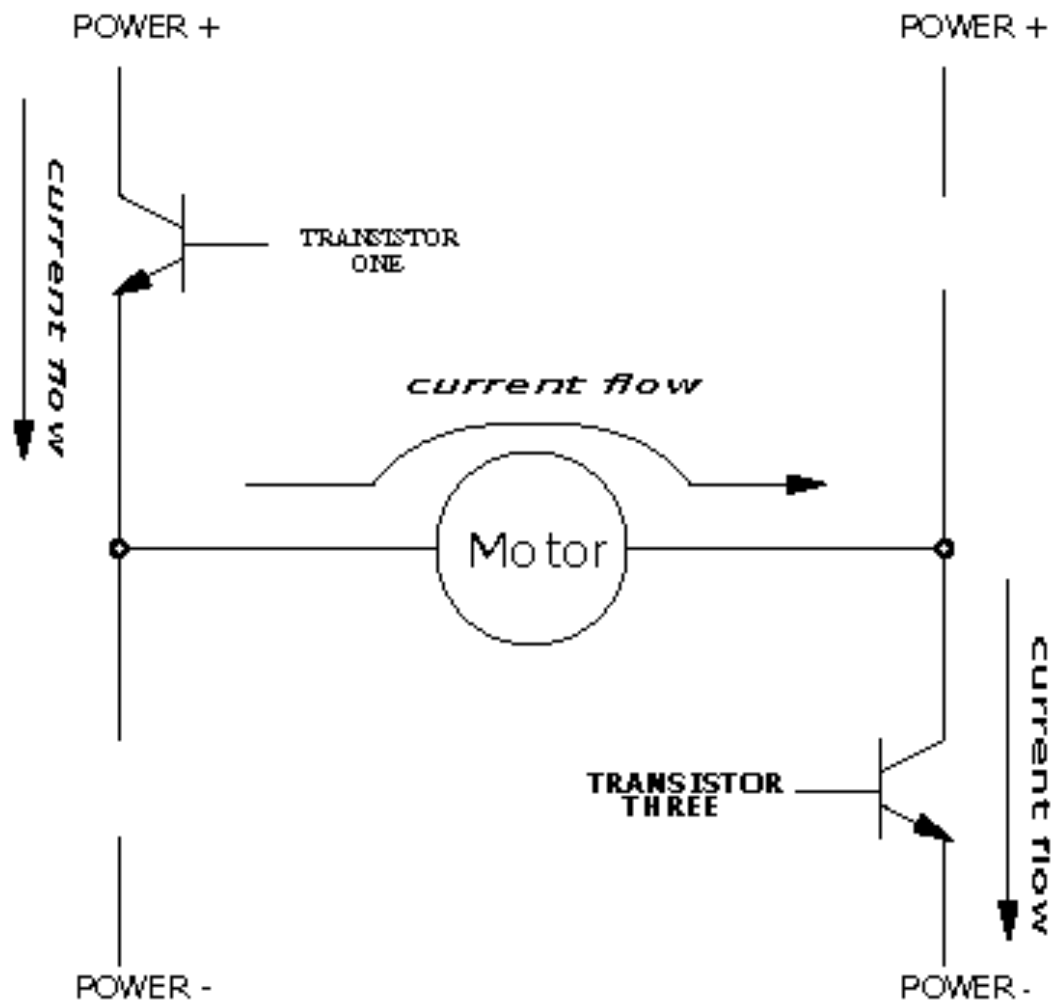
INSIDE A SPST RELAY

pic r-1a

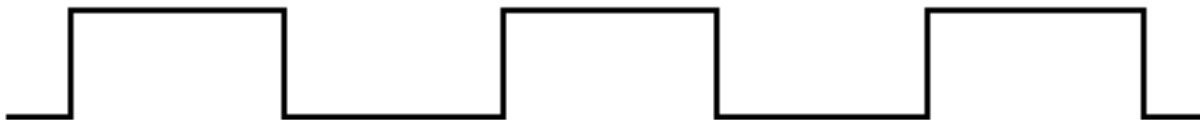


H-bridge





1a: 1:1 mark-space ratio (50% duty cycle)



1b: 3:1 mark-space ratio (75% duty cycle)



1c: 1:3 mark-space ratio (25% duty cycle)



Figure 1: Pulse width modulation waveforms

The speed of the motor is controlled by pulse width modulation (PWM), as shown in the diagram in Figure 3-5. The motor power is rapidly turned on and off over a time interval. The speed of a motor depends on the average voltage applied to it, and the PWM method is a way of controlling this average voltage. It is energy efficient because the transistors are either completely off or on.

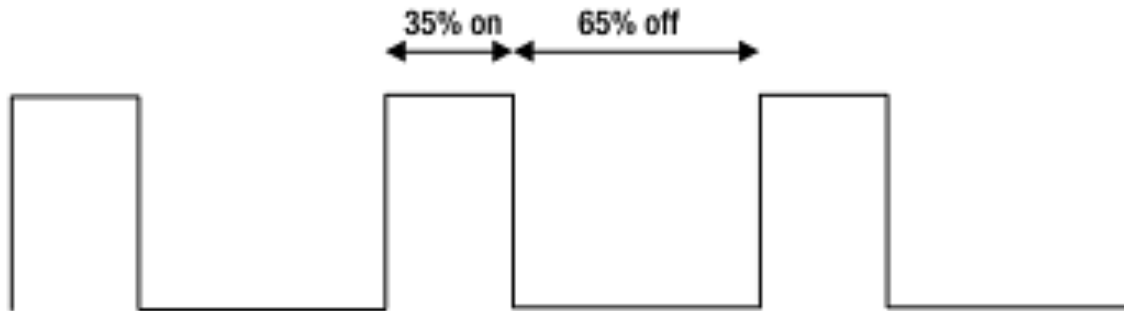


Figure 3-5. PWM for motor at power level of 35%

With the standard firmware, the length of the whole cycle is $128\mu\text{s}$. This corresponds to 7,800Hz,

$$\text{voltage} = \text{duty cycle} * 9 \text{ volt}$$

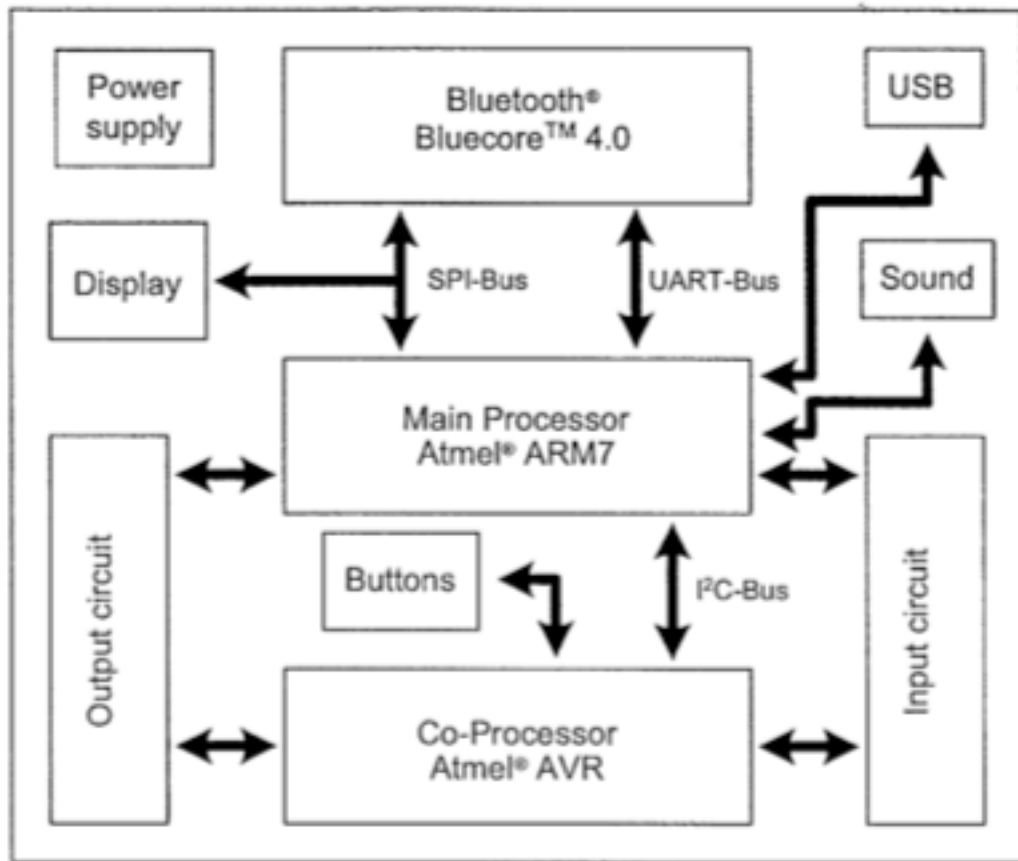
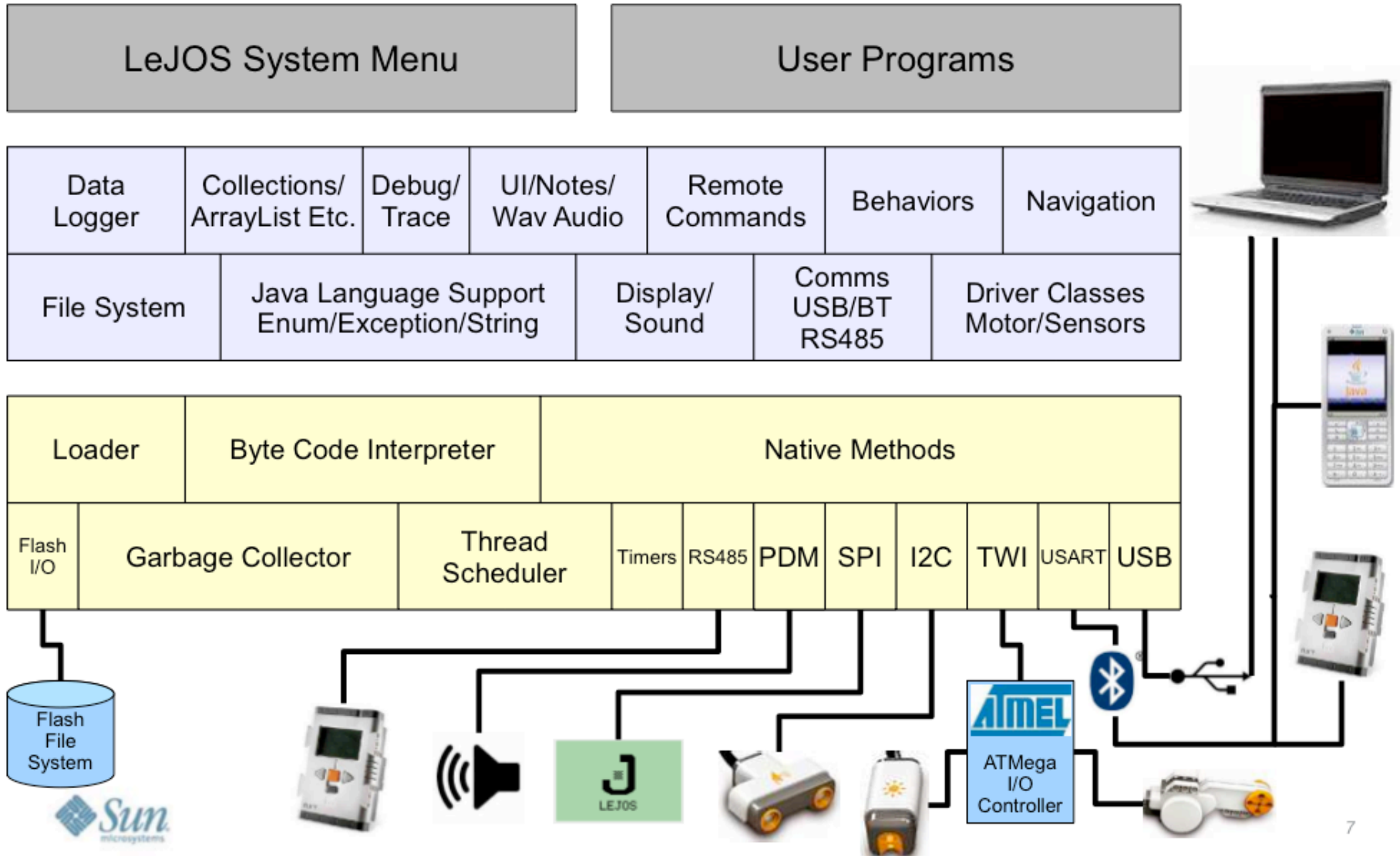
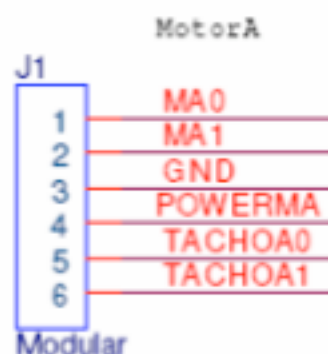


Figure 1: Hardware block diagram of the NXT brick

LeJOS Architecture





Pin 1, MA0

PWM output signal for the actuators

Pin 2, MA1

PWM output signal for the actuators

Pin 3, GND

Ground signal related to the output supply

Pin 4, POWERMA

4.3 Volt output supply

Pin 5, TACHOA0

Input value that includes Schmitt trigger functionality

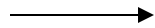
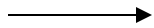
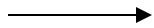
Pin 6, TACHOA1

Input value that includes Schmitt trigger functionality

analog quantity,
e.g. light

digital quantity,
e.g. light %

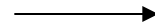
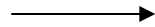
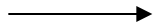
stimuli



sensor

interface

control program



response

control program

interface

actuator

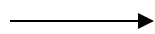
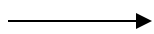
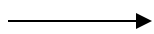
digital quantity,
e.g. power %

analog quantity,
e.g. pulse train

analog quantity,
e.g. light

digital quantity,
e.g. light %

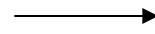
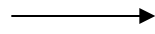
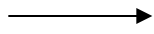
stimuli



sensor

interface

control program



response

control program

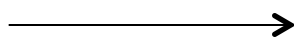
interface

actuator

digital quantity,
e.g. power %

analog quantity,
e.g. pulse train

sensor space



actuator space

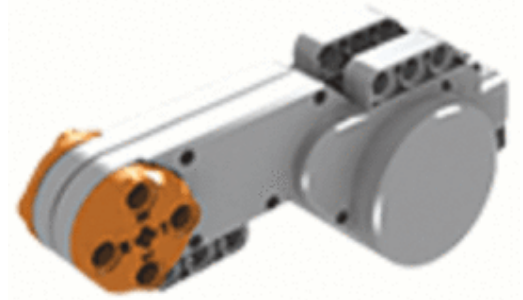
Embedded Java

The leJOS API classes provide access to the hardware. Especially the output ports and actuators:

MotorPort

Motor

DifferentialPilot



lejos.nxt

Class MotorPort

[java.lang.Object](#)

└─ `lejos.nxt.MotorPort`

All Implemented Interfaces:

[BasicMotorPort](#), [TachoMotorPort](#), [Encoder](#)

```
public class MotorPort
extends Object
implements TachoMotorPort
```

Abstraction for a NXT output port.

Field Summary	
static MotorPort	A MotorPort A.
static MotorPort	B MotorPort B.
static MotorPort	C MotorPort C.

Method Summary

void	<code>controlMotor</code> (int power, int mode) Low-level method to control a motor.
int	<code>getId</code> ()
static MotorPort	<code>getInstance</code> (int id) Return the MotorPort with the given Id.
int	<code>getTachoCount</code> () returns tachometer count
void	<code>resetTachoCount</code> () resets the tachometer count to 0;
void	<code>setPWMMode</code> (int mode)

controlMotor

```
public void controlMotor(int power,  
                        int mode)
```

Low-level method to control a motor.

Specified by:

[`controlMotor`](#) in interface [BasicMotorPort](#)

Parameters:

power - power from 0-100

mode - defined in [BasicMotorPort](#). 1=forward, 2=backward, 3=stop, 4=float.

```
package lejos.nxt;

/**
 *
 * Abstraction for a NXT output port.
 *
 */
public class MotorPort implements TachoMotorPort {
    private int _id;
    private int _pwmMode = PWM_FLOAT; // default to float mode

    private MotorPort(int id)
    {
        _id = id;
    }

    /**
     * The number of ports available.
     */
    public static final int NUMBER_OF_PORTS = 3;

    /**
     * MotorPort A.
     */
    public static final MotorPort A = new MotorPort (0);

    /**
     * MotorPort B.
     */
    public static final MotorPort B = new MotorPort (1);

    /**
     * MotorPort C.
     */
    public static final MotorPort C = new MotorPort (2);
}
```

```

/**
 * Low-level method to control a motor.
 *
 * @param power power from 0-100
 * @param mode defined in <code>BasicMotorPort</code>. 1=forward, 2=backward, 3=stop, 4=float.
 * @see BasicMotorPort#FORWARD
 * @see BasicMotorPort#BACKWARD
 * @see BasicMotorPort#FLOAT
 * @see BasicMotorPort#STOP
 */
public void controlMotor(int power, int mode)
{
    // Convert lejos power and mode to NXT power and mode
    controlMotorById(_id,
                    (mode >= 3 ? 0 : (mode == 2 ? -power: power)) ,
                    (mode == 3 ? 1 : (mode == 4 ? 0 : _pwmMode)));
}

```

lejos.nxt

Class Motor

[java.lang.Object](#)

└─ `lejos.nxt.Motor`

```
public class Motor  
extends Object
```

Motor class contains 3 instances of regulated motors.

Example:

```
Motor.A.setSpeed(720); // 2 RPM  
Motor.C.setSpeed(720);  
Motor.A.forward();  
Motor.C.forward();  
Thread.sleep (1000);  
Motor.A.stop();  
Motor.C.stop();  
Motor.A.rotateTo( 360);  
Motor.A.rotate(-720,true);  
while(Motor.A.isMoving() :Thread.yield());  
int angle = Motor.A.getTachoCount(); // should be -360  
LCD.drawInt(angle,0,0);
```


Class NXTRegulatedMotor

[java.lang.Object](#)└─ [lejos.nxt.NXTRegulatedMotor](#)

All Implemented Interfaces:

[BaseMotor](#), [Encoder](#), [RegulatedMotor](#), [Tachometer](#)

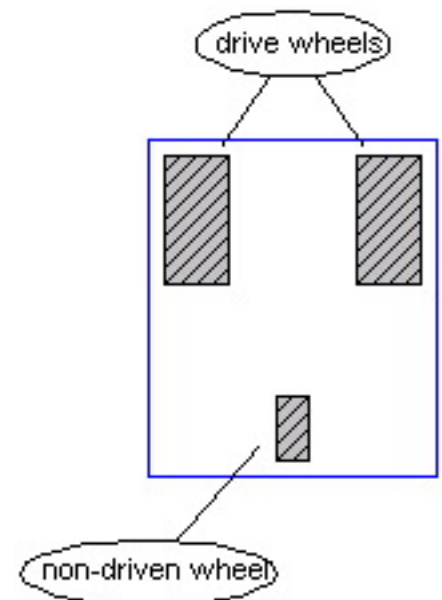
void	rotate (int angle) Rotate by the requested number of degrees.
void	rotate (int angle, boolean immediateReturn) Rotate by the request number of degrees.
void	rotateTo (int limitAngle) Rotate to the target angle.
void	rotateTo (int limitAngle, boolean immediateReturn) causes motor to rotate to limitAngle; if immediateReturn is true, method returns immediately and the motor stops by itself and getTachoCount should be within +- 2 degrees if the limit angle If any motor method is called before the limit is reached, the rotation is canceled.
void	backward () Causes motor to rotate backwards until <code>stop()</code> or <code>flt()</code> is called.
void	flt () Set the motor into float mode.
void	flt (boolean immediateReturn) Set the motor into float mode.
void	forward () Causes motor to rotate forward until <code>stop()</code> or <code>flt()</code> is called.

lejos.robotics.navigation

Class DifferentialPilot

[java.lang.Object](#)

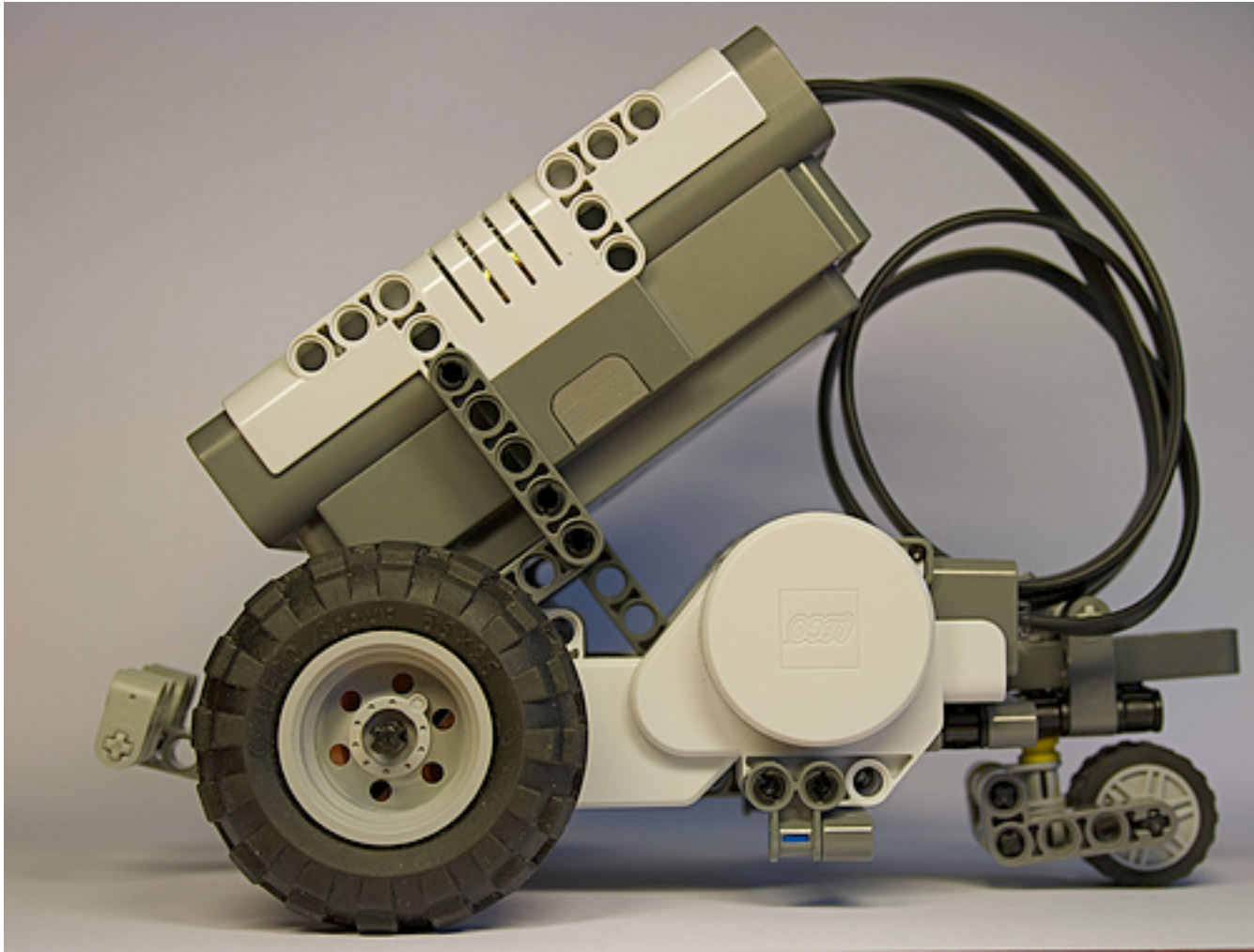
└─ `lejos.robotics.navigation.DifferentialPilot`



```
DifferentialPilot pilot = new DifferentialPilot(2.1f, 4.4f, Motor.A, Motor.C, true); // parameters in inches
pilot.setRobotSpeed(30); // cm per second
pilot.travel(50); // cm
pilot.rotate(-90); // degree clockwise
pilot.travel(-50,true); // move backward for 50 cm
while(pilot.isMoving())Thread.yield();
pilot.rotate(-90);
pilot.rotateTo(270);
pilot.steer(-50,180,true); // turn 180 degrees to the right
waitComplete(); // returns when previous method is complete
pilot.steer(100); // turns with left wheel stationary
Delay.msDelay(1000);
pilot.stop();
```

Differential Drive

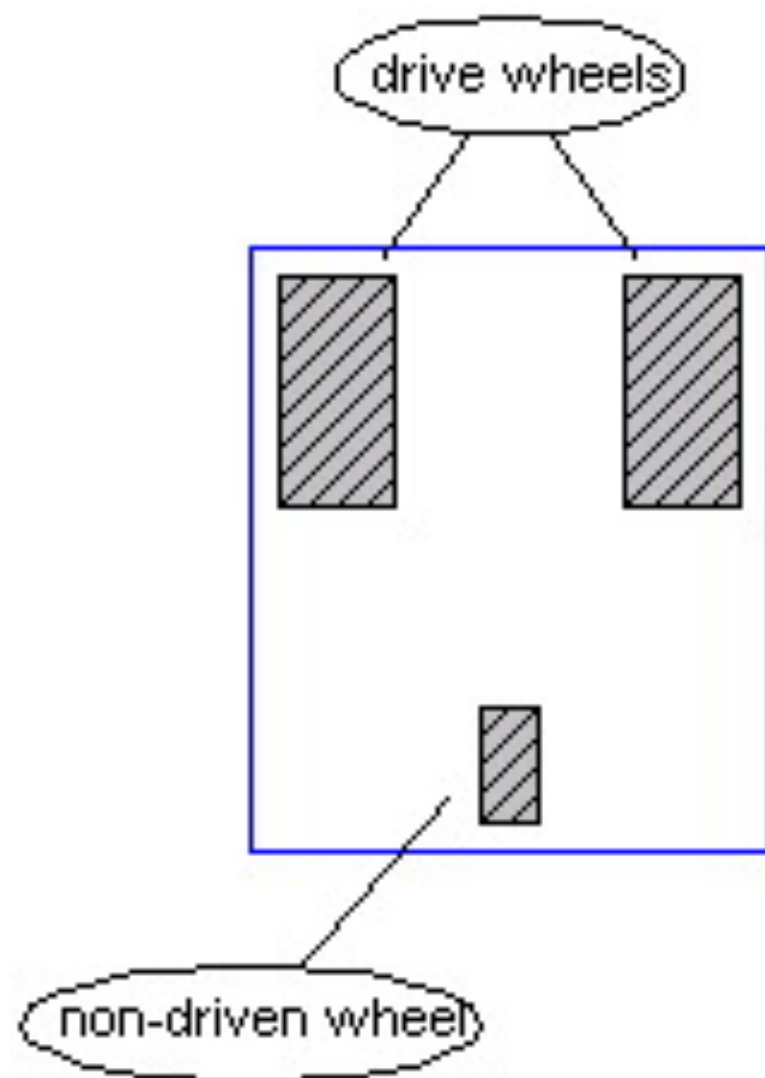
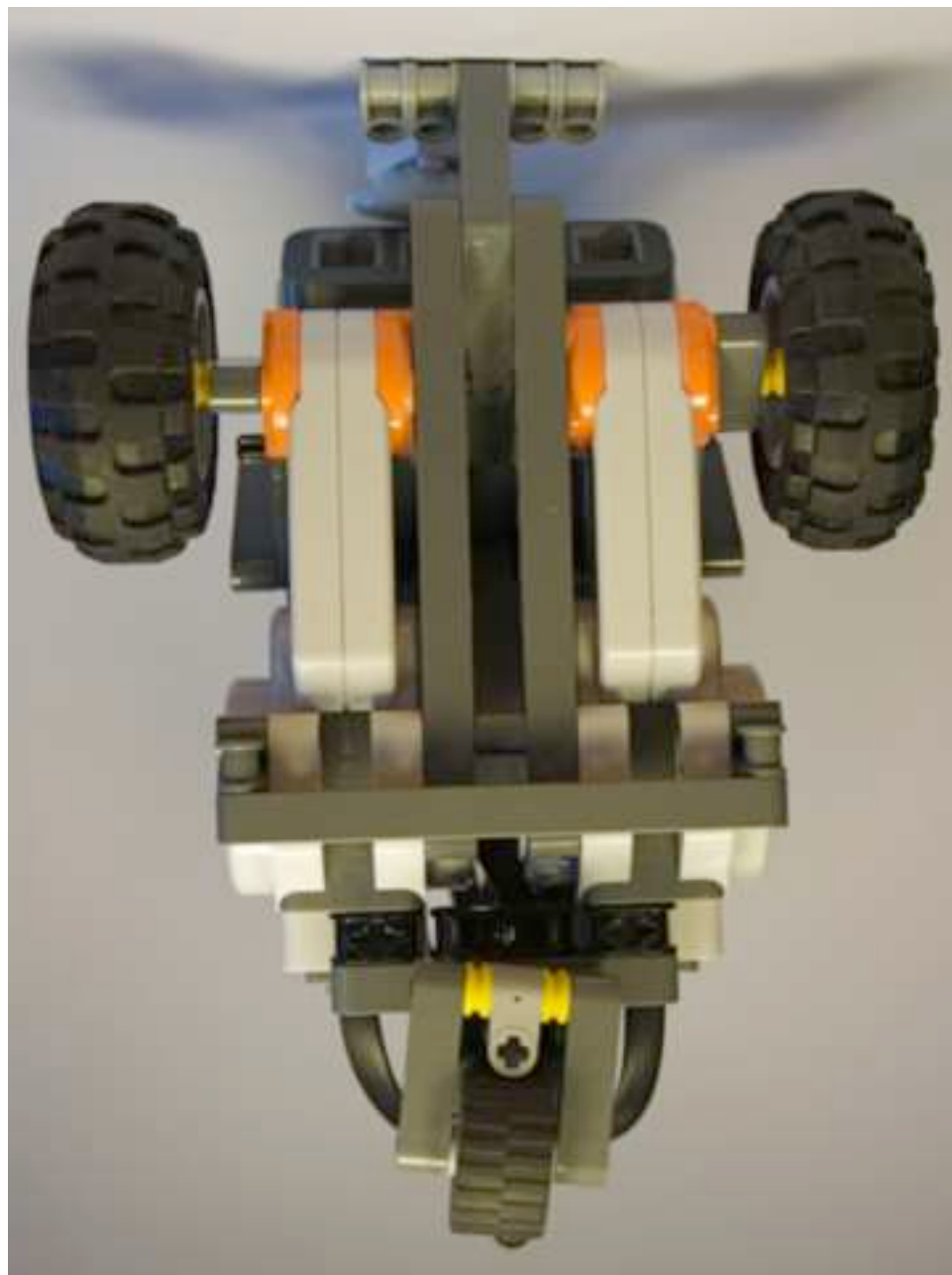




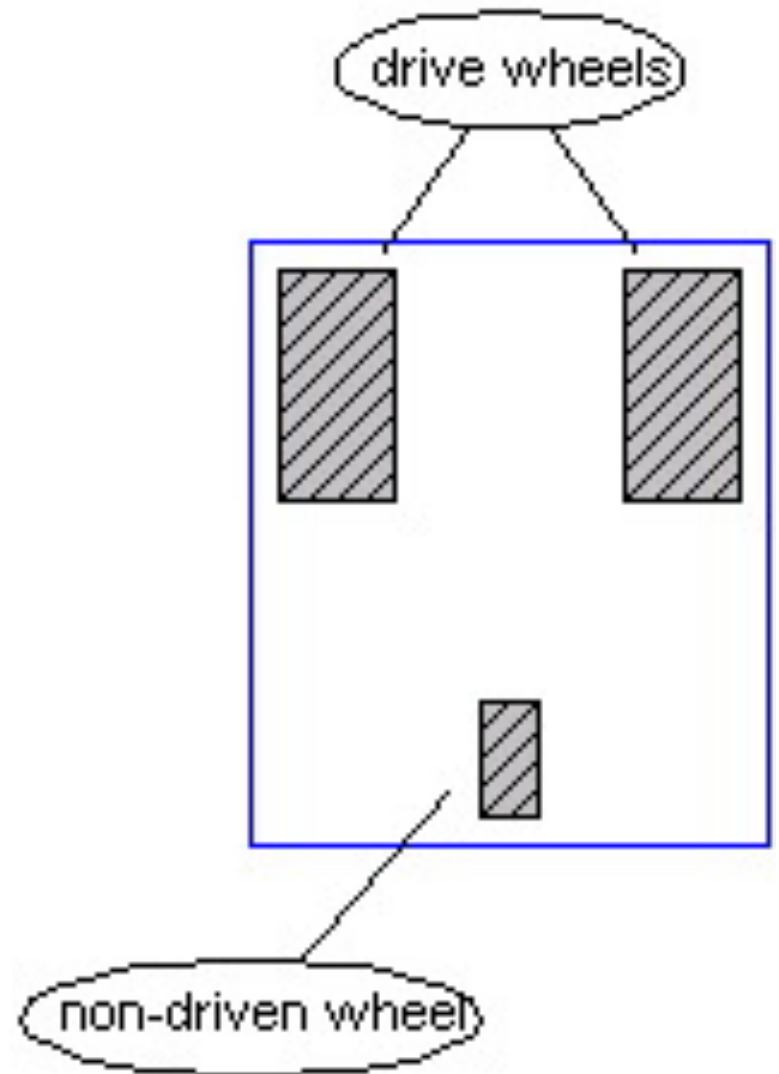
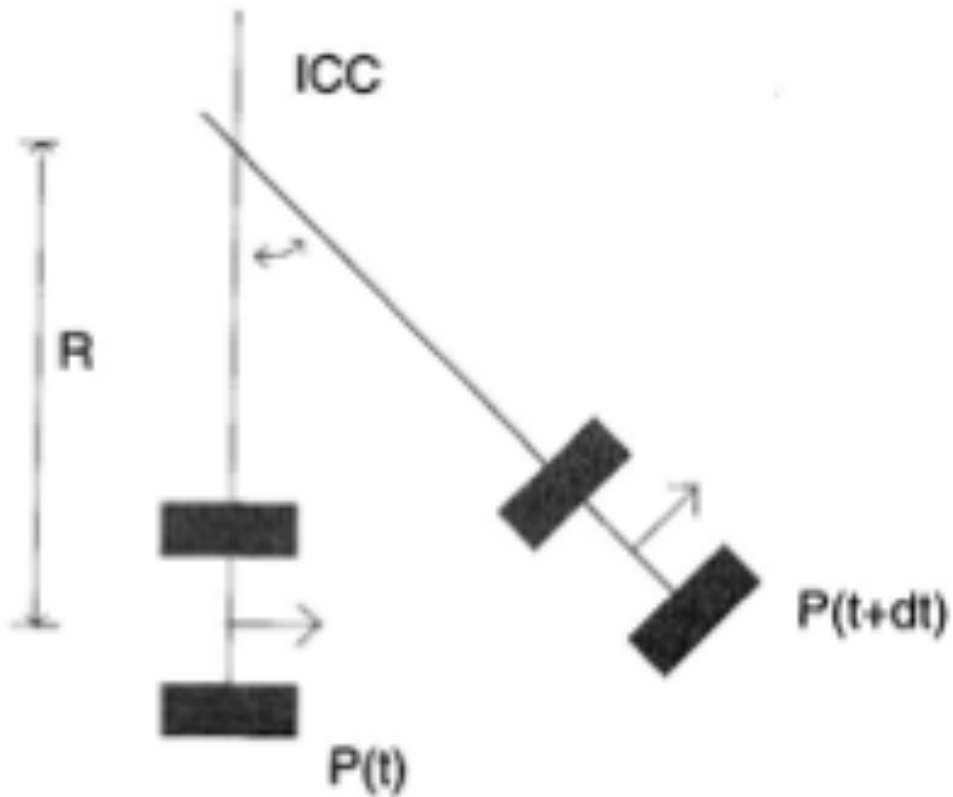
Forward ←



Backward



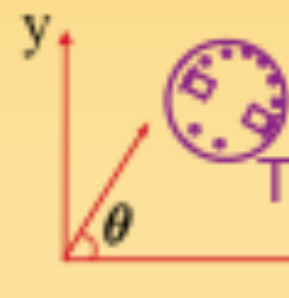
Instantaneous Center of Curvature



Forward kinematics

Task:

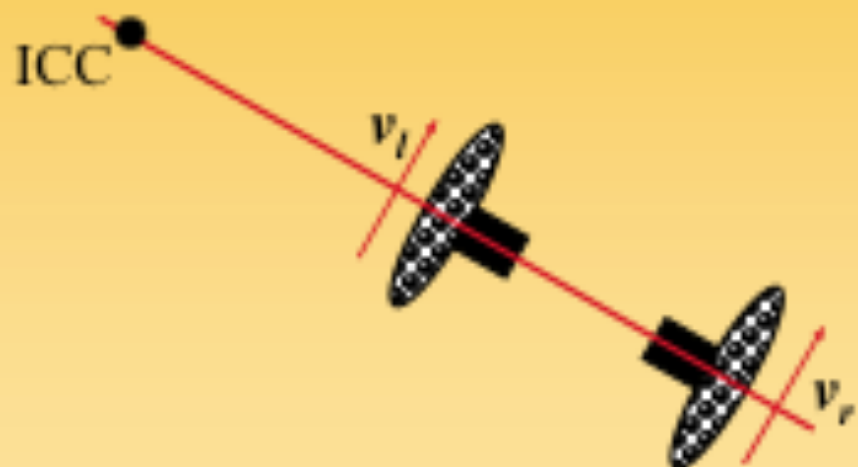
Standing in **the pose** (x, y, θ) at time t ,
Determine the pose (x', y', θ') at time $t + \delta t$
given the control parameters (v_r, v_l) !



The pose (x, y, θ) is defined in a global coordinate system

Differential drive

- Pairs of wheels mounted on a common axis
- If the wheels are rotating on the ground:
There is a point ICC !
- By varying (v_r, v_l) , ICC moves and different trajectories are chosen

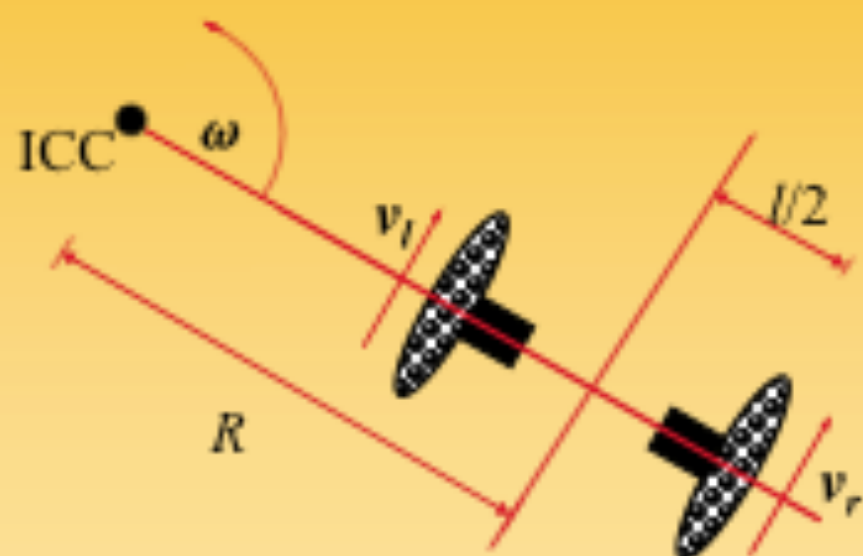


Angular velocity ω

For left and right wheel:

1) $\omega (R+l/2) = v_r$

2) $\omega (R - l/2) = v_l$



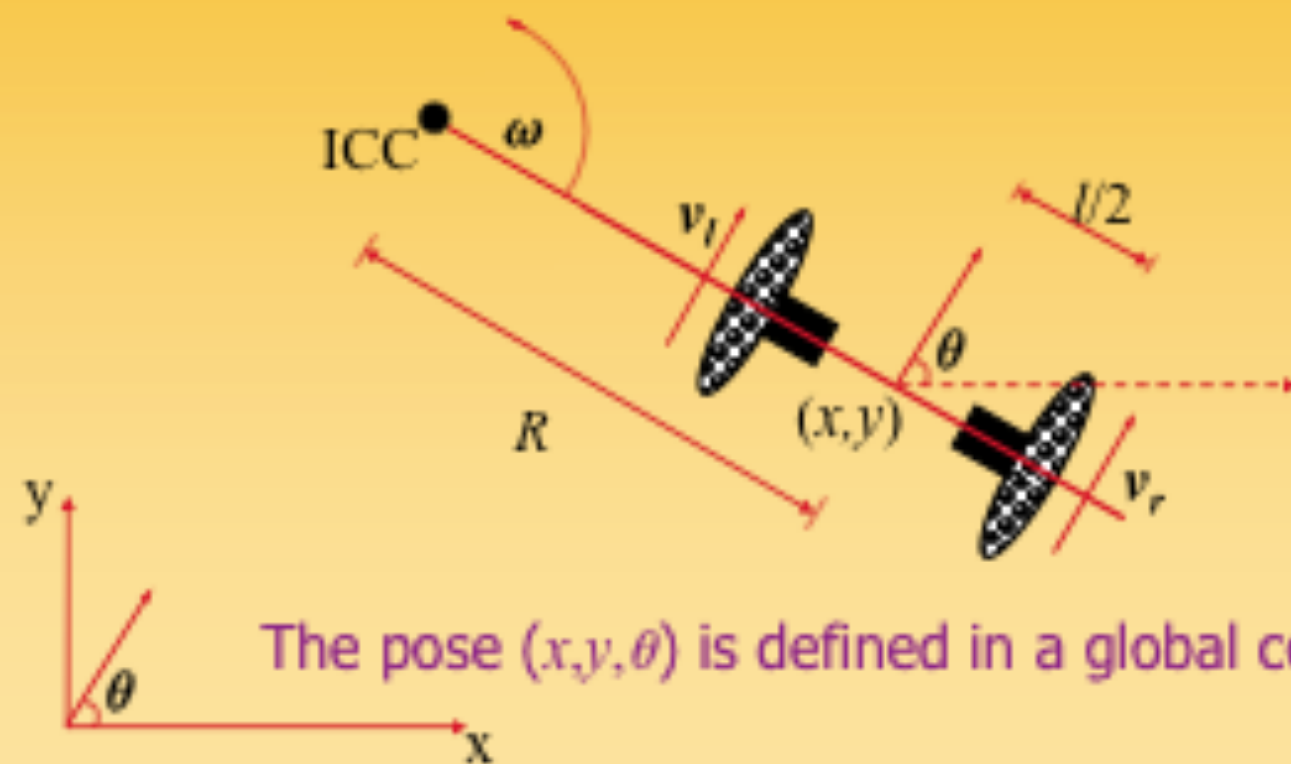
Solve for ω and R :

3) $R = l/2(v_l + v_r) / (v_r - v_l)$

4) $\omega = (v_r - v_l) / l$

Forward kinematics

Standing in the pose (x, y, θ) at time t ,
determine the pose (x', y', θ') at time $t + \delta t$
given the control parameters (v_r, v_l) !



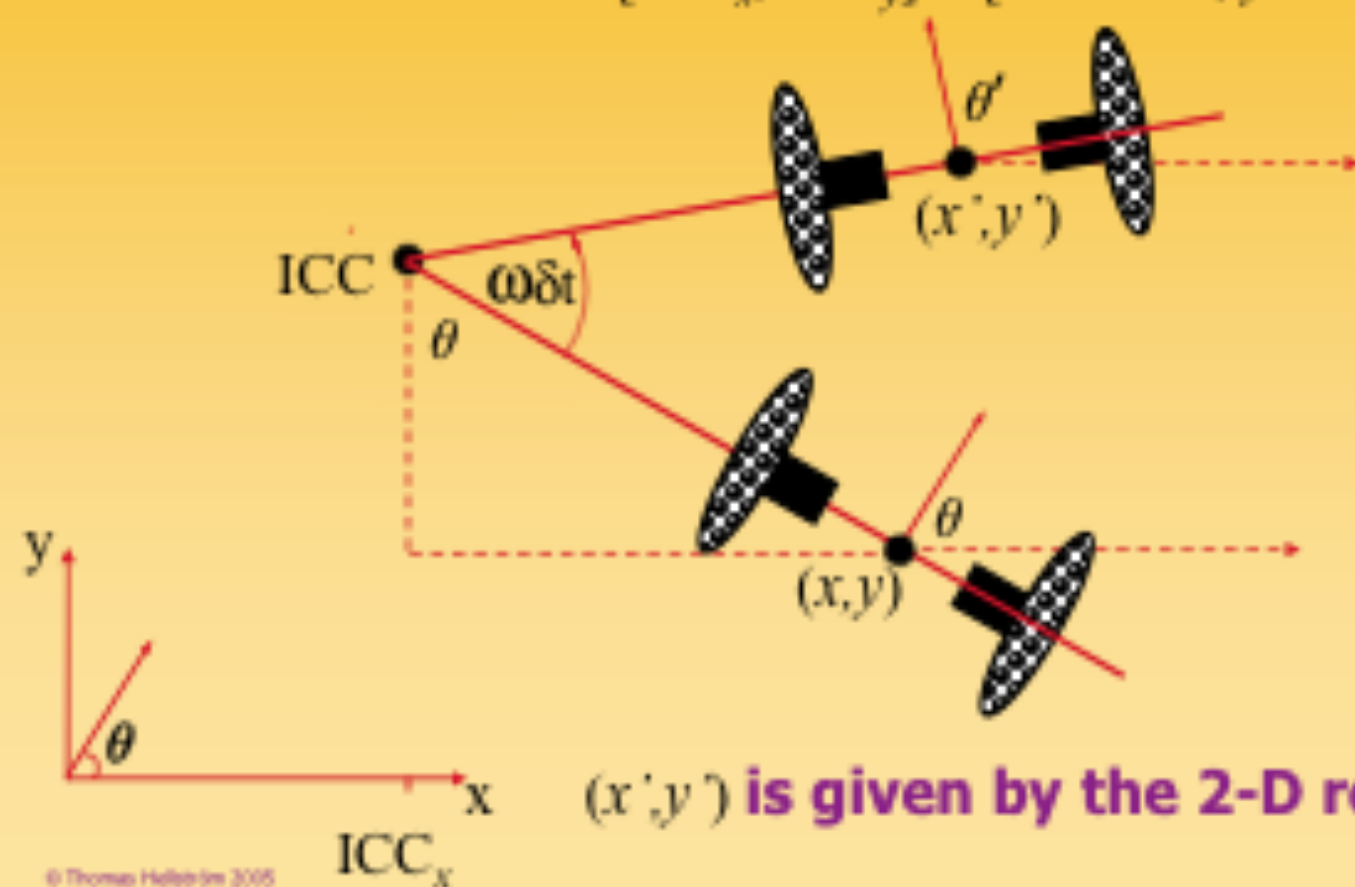
The pose (x, y, θ) is defined in a global coordinate system

Forward kinematics

Rotate around ICC with angular velocity ω for δt seconds:

$$\theta' = \omega \delta t + \theta.$$

$$\text{ICC} = [\text{ICC}_x, \text{ICC}_y] = [x - R \sin \theta, y + R \cos \theta].$$



(x', y') is given by the 2-D rotational matrix:

Forward kinematics

Rotate around ICC with angular velocity ω for δt seconds:

Position at time $t + \delta t$:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\omega\delta t) & -\sin(\omega\delta t) \\ \sin(\omega\delta t) & \cos(\omega\delta t) \end{bmatrix} \begin{bmatrix} x - \text{ICC}_x \\ y - \text{ICC}_y \end{bmatrix} + \begin{bmatrix} \text{ICC}_x \\ \text{ICC}_y \end{bmatrix}$$

Wheel encoders give decoder counts n_r and n_l from time t to $t + \delta t$.

In general: $n \text{ step} = v \delta t \Rightarrow v = n \text{ step} / \delta t$

where *step* is the length (mm) of one decoder tick.

Insert in 3) and 4):

$$R = l/2(v_l + v_r) / (v_r - v_l) = l/2(n_l + n_r) / (n_r - n_l)$$

$$\omega\delta t = (v_r - v_l) \delta t / l = (n_r - n_l) \text{step} / l$$

Inverse kinematics

Task:

Standing in **the pose** (x, y, θ) at time t ,
Determine control parameters (v_r, v_l) such
that the pose is (x', y', θ') at time $t + \delta t$
Often infinitely many solutions.
Hard to find the optimal solution.

Often easy to find **ONE** solution by
decomposing the problem and
controlling only a few DOF at a time

Inverse kinematics

For the Khepera

$$v_r = v_l \Rightarrow$$

$$n_r = n_l \Rightarrow R = \infty, \omega \delta t = 0$$

The robot will move in a straight line. I.e.: θ remains the same

$$v_r = -v_l \Rightarrow$$

$$n_r = -n_l \Rightarrow R = 0, \omega \delta t = 2n_l \text{step} / l$$

$$\text{ICC} = [\text{ICC}_x, \text{ICC}_y] = [x, y].$$

$$x' = x, y' = y, \theta' = \theta + \omega \delta t$$

The robot will rotate in place about ICC. I.e.: any θ is reachable.

(x,y) remains the same

NXT Programming



Lesson 3

